

**Question 8** (12 marks) Use a SEPARATE writing booklet.

- (a) A drug is used to control a medical condition. It is known that the quantity  $Q$  of drug remaining in the body after  $t$  hours satisfies an equation of the form

$$Q = Q_0 e^{-kt}$$

where  $Q_0$  and  $k$  are constants.

The initial dose is 6 milligrams and after 15 hours the amount remaining in the body is half the initial dose.

- (i) Find the values of  $Q_0$  and  $k$ . **3**
- (ii) When will one-eighth of the initial dose remain? **2**
- (b) A particle moves in a straight line. At time  $t$  seconds, its distance  $x$  metres from a fixed point  $O$  on the line is given by

$$x = \sin 2t + 3.$$

- (i) Sketch the graph of  $x$  as a function of  $t$  for  $0 \leq t \leq 2\pi$ . **3**
- (ii) Using your graph, or otherwise, find the times when the particle is at rest, and the position of the particle at those times. **2**
- (iii) Describe the motion completely. **2**