2010 HSC Mathematics

Question 3 (12 marks) Use the Question 3 Writing Booklet.

(a) In the diagram A, B and C are the points (-2, -4), (12, 6) and (6, 8) respectively. The point N(2, 2) is the midpoint of AC. The point M is the midpoint of AB.



(i)	Find the coordinates of <i>M</i> .	1
(ii)	Find the gradient of <i>BC</i> .	1
(iii)	Prove that $\triangle ABC$ is similar to $\triangle AMN$.	2
(iv)	Find the equation of MN.	2
(v)	Find the exact length of <i>BC</i> .	1
(vi)	Given that the area of $\triangle ABC$ is 44 square units, find the perpendicular distance from A to BC.	1

Question 3 continues on page 5

2010 HSC Mathematics

Question 3 (continued)

- (b) (i) Sketch the curve $y = \ln x$. 1
 - (ii) Use the trapezoidal rule with three function values to find an **2** approximation to

$$\int_{1}^{3} \ln x \, dx.$$

(iii) State whether the approximation found in part (ii) is greater than or 1 less than the exact value of $\int_{1}^{3} \ln x \, dx$. Justify your answer.

End of Question 3