

Start here for  
Question Number: **4**

(a) 26 weeks

week 1  $\rightarrow$  1 km

week 2  $\rightarrow$  1 km + 750 m

week 3  $\rightarrow$  1 km + 1500

⋮

week n  $\rightarrow$  10 km

(i)  $1 + 1.75 + 2.5 + \dots + 10$

$$\frac{T_2}{T_1} = \frac{T_3}{T_2} = \frac{1.75}{1} = \frac{2.5}{1.75}$$

$$T_2 - T_1 = T_3 - T_2$$

$$1.75 - 1 = 2.5 - 1.75 : \text{AP.}$$

$$T_n = a + (n-1)d$$

$$T_9 = 1 + (9-1)0.75$$

$$= 1 + 6$$

$$= 7 \text{ km's}$$

$$10 = 1 + (n-1)0.75$$

$$10 = 1 + 0.75n - 0.75$$

$$10 = 0.75n + 0.25$$

$$0.75n = 9.75$$

$$n = 13$$

∴ after 13 weeks on week 13 she runs 10 km for the first time.

$$(iii) S_n = \frac{n}{2}(a + l)$$

$$S_n = \frac{n}{2}(2a + (n-1)d)$$

~~$$S_{26} = \frac{26}{2}(1 + 10) + S_{13} = \frac{26}{2}(2(1) + (26-1)0.75)$$~~

$$S_{13} = \frac{13}{2}(1 + 10) = 71.5 \text{ km} +$$

~~$$S_{13} = \frac{13}{2}(2(1) + (13-1)0.75)$$~~

$$S_{13} = \frac{13}{2}(2(1) + (13-1)0.75)$$

$$= 91$$

∴ she travels 162.5 km over 26 weeks.

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(b)

$$\int_0^2 e^{2x} - e^{-x} dx$$

$$= [2e^{2x} + e^{-x}]_0^2$$

$$= [(2e^{4} + e^{-2}) - (2e^{0} + e^{-1})]$$

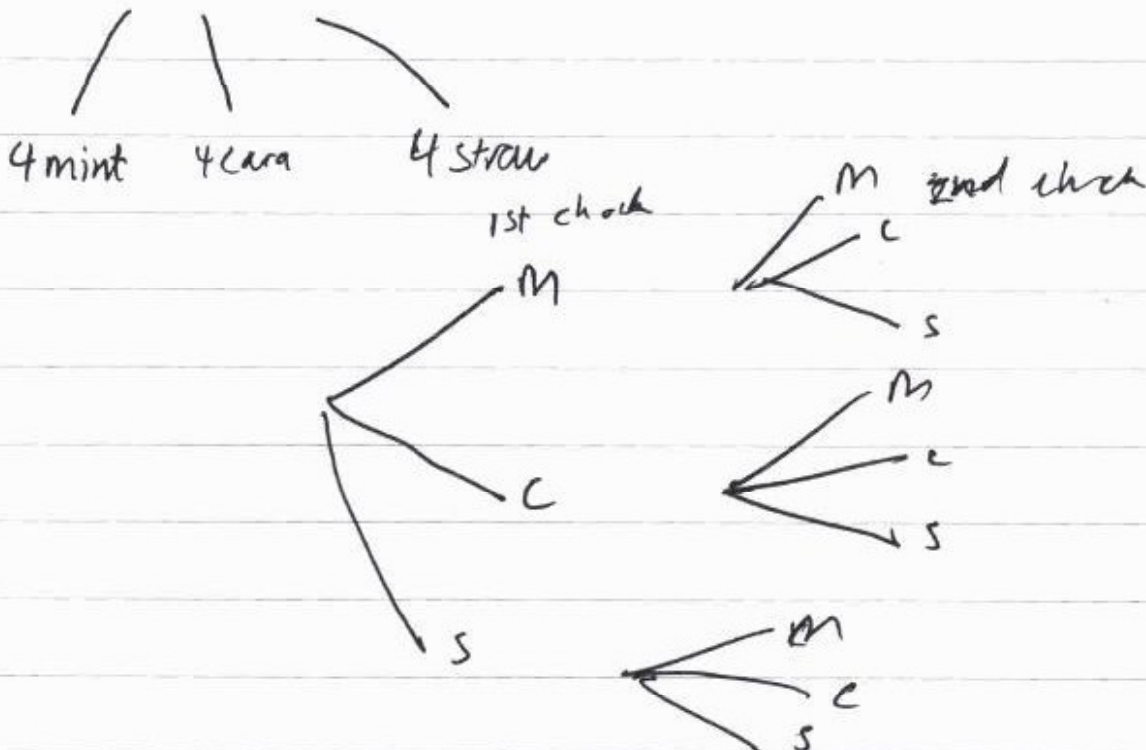
$$= 2e^4 + e^{-2} - 2 + 1$$

$$A = (2e^4 + e^{-2} - 1) u^2 \quad \text{for } u = e^2$$

~~$$A = 2u^3 + u^1$$

$$= 2u^2 + \frac{u}{x} - x$$~~

(c) 12 choc



You may ask for an extra Writing Booklet if you need more space to answer question 4.



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$$MM = \frac{1}{4} \times \frac{1}{3} = \frac{1}{12}$$

$$(ii) \quad \frac{1}{4} \times \frac{1}{8} = \frac{1}{32}$$

$$(iii) \quad \frac{1}{4} \times \frac{1}{11} = \frac{1}{44}$$

$$(a) \quad f(x) = 1 + e^x$$

$$(1 + e^x) \times - (1 + e^x) = (1 + e^x) - (1 + e^x)$$

$$(1 + e^x)(-1 - e^x) = (1 + e^x) - (1 + e^x)$$

$$-1 - e^x - e^x - e^{2x} = 1 + e^x - 1 - e^x$$

$$-1 - 2e^x - e^{2x} = 0$$

$$0 = e^{2x} + 2e^x + 1 \quad \text{let } u = e^x$$

$$\begin{aligned}\therefore 0 &= u^2 + 2u + 1 \\ &= (u+1)(u+1)\end{aligned}$$

$$u = -1$$

$$\therefore e^x = -1$$

~~no solution~~

$$\therefore x = 0$$

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