

Start here for

Question Number:

6

$$\begin{aligned}
 \text{a) (i) } f(x) &= (x+2)(x^2+4) \\
 &= x^3 + 4x + 2x^2 + 8 \\
 f'(x) &= 3x^2 + 4 + 4x \\
 &= 3x^2 + 4x + 4 \\
 &= \text{[scribbled out]}
 \end{aligned}$$

\therefore no possible stationary points, as;

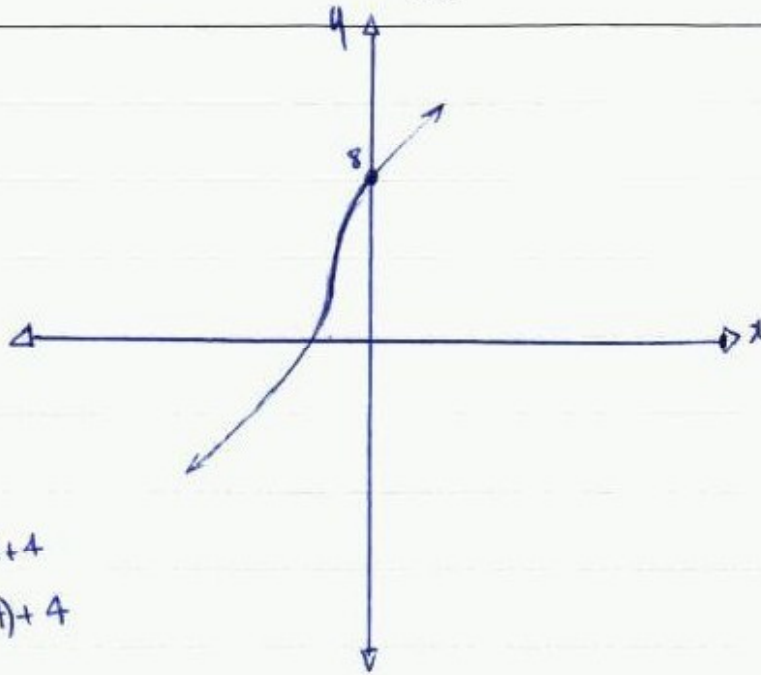
$$\begin{aligned}
 x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\
 &= \frac{-4 \pm \sqrt{16 - 4(3)(4)}}{2(3)} \\
 &= \frac{-4 \pm \sqrt{-32}}{6}
 \end{aligned}$$

\therefore No stationary points exist on the curve.

$$\begin{aligned}
 \text{(ii) } y &= f(x) \\
 y' &= 3x^2 + 4 + 4x \\
 y'' &= 6x + 4 \\
 6x &= -4 \\
 x &= -\frac{2}{3}
 \end{aligned}$$

\therefore when $x \geq -\frac{2}{3}$ the graph concave down, and $x < -\frac{2}{3}$ the graph is concave up.

(ii)



$$\begin{aligned} x - \text{int} &= 3x^2 + 4x + 4 \\ &= x(3x + 4) + 4 \\ &= \end{aligned}$$

$$(b) (i) \angle POQ = \theta = r\theta$$

$$9 = 5\theta$$

$$\theta = \frac{9}{5} \times \frac{\pi}{180}$$

$$= \frac{9\pi}{5}$$

(ii) In $\triangle OPT$ and $\triangle OQT$:

$OP = OQ = 5$ cm (radii of circle.)

$\angle OPQ = \angle OQP = 90^\circ$ (given)

$OT = OT = \text{bisector}$ (common)

\therefore due to SAS $\triangle OPT \cong \triangle OQT$

(iii)



$$\tan\left(\frac{9\pi}{5}\right) = \frac{PT}{5}$$

$$\tan\left(\frac{18\pi}{5}\right) = \frac{PT}{5}$$

$$PT = 6.499\dots$$

\therefore PT is 6.5 cm Additional writing space on back page.

$$\begin{aligned} \text{(iv) } A &= \frac{1}{2} r^2 (\theta - \sin \theta) \\ &= \frac{1}{2} \cdot 5^2 \left(\frac{9\pi}{5} - \sin \frac{9\pi}{5} \right) \\ &= \frac{25}{2} \left(\frac{9\pi}{5} - \sin \frac{9\pi}{5} \right) \end{aligned}$$

$$= \frac{22\pi}{10} - \frac{\sin 22\pi}{10}$$

= Area of sector

Hence,

Area of kite:

$$\begin{aligned} &\frac{1}{2} \times y \times x \\ &= \frac{1}{2} \times 8.2 \times x \\ &= 4.1x \end{aligned}$$

$$\therefore 4.1x - \frac{22\pi}{10} - \frac{\sin 22\pi}{10} = \text{Shaded region}$$

