

Start here for
Question Number: **8**

$$a) \frac{dp}{dt} = kP.$$

~~$$105e^{kt} = Ae^{kt}$$~~

~~$$105e^{k \cdot 75} = 105e^{k \cdot 75} = 200000000.$$~~

~~$$k \cdot 75 = \ln \frac{200000000}{105}$$~~

$$k = 0.162097 \dots$$

$$105e^{0.162097 \cdot 100} = \text{pop in 2035.}$$

$$= 1150739165 \text{ cars roads in 2035.}$$

b) both starting heads = 0.36. ~~2 per~~

1 starting heads = ~~2 per~~

2 tails =

$$\begin{array}{l} \text{HH} \quad 0.36 \\ \text{HT} \quad + \\ \text{TH} \quad 2 \\ \text{TT} \end{array}$$

b) 2 heads = 0.36

other possibilities = 0.64.

$$\begin{array}{l} \text{H} \begin{cases} \text{H} \quad 0.36 \\ \text{T} \quad 0.6 \end{cases} \\ \text{T} \begin{cases} \text{H} \\ \text{T} \end{cases} \end{array}$$

$$1 \text{ heads} = \sqrt{0.36} = 0.6.$$

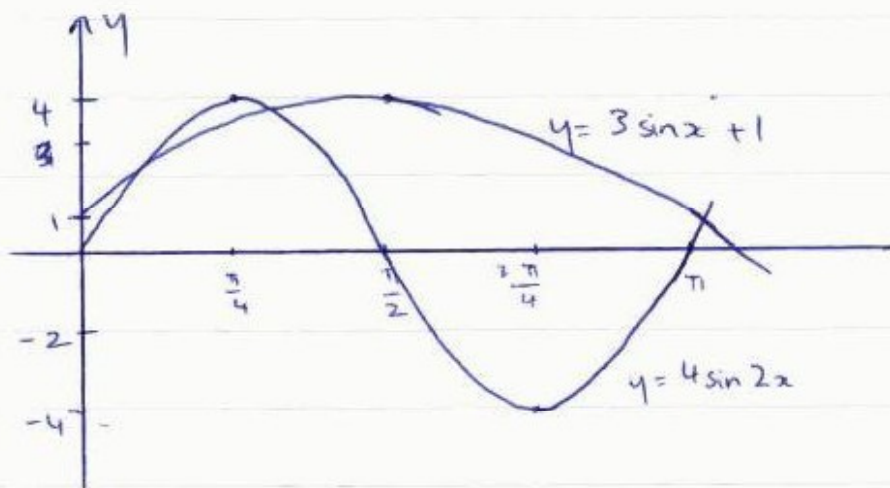
so 2 tails = 0.04.

c) i) 4

ii) $\frac{2\pi}{b} = \pi$

= 2.

iii



d) $f'(x) = 3x^2 - 6x + k$

increasing where $f'(x) > 0$

$$3x^2 - 6x + k > 0$$

~~$$3x^2 - 6x + k > 0$$~~

~~$$3x^2 - 6x + k > 0$$~~

$$3x^2 - 6x > -k$$

$$3x(x - 2) > -k$$

$$0, 2 > -k$$

$$k > -2, 0.$$

Additional writing space on back page.